

Name: _____
Date: _____

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Exponential Functions – 08
Practice Test 03

1. In 1984, Maggie bought a house worth \$ 220 000 but did no maintenance on it.
As a result, the value of the house **depreciated** by 4.5% every year since the time she bought it.

How much is the house worth in 2016?

$$\begin{aligned}x &= \text{years} \quad \frac{2016}{1984} = 32 \\y &= \text{value} \\a &= 220\,000 \\c &= 100 - 4.5 = \frac{95.5}{100} = 0.955\end{aligned}$$

$$\begin{aligned}y &= ac^x \\y &= 220\,000 (0.955)^{32} \\y &= 50\,411.61\end{aligned}$$

/ 3 pts

The house is worth \$ 50 411.61

2. **Three** mutant dogs are created in a lab and escape containment.

If the population of mutant dogs **doubles** every day, **how many mutant dogs will exist after two weeks?**

$$\begin{aligned}x &= \text{days} (14) \\y &= \text{dogs} \\a &= 3 \\c &= 2\end{aligned}$$

$$\begin{aligned}y &= ac^x \\y &= 3(2)^{14} \\y &= 49\,152\end{aligned}$$

/ 3 pts

There will be 49 152 mutant dogs

3. The ultimate 'rock-paper-scissors' competition has drawn **8192 players** from across the world.
After each round, **half** of the players are eliminated.

How many players will be left after the 12th round?

$$\begin{aligned}x &= \text{rounds} (12) \\y &= \text{players} \\a &= 8192 \\c &= \frac{100 - 50}{100} = 0.5\end{aligned}$$

$$\begin{aligned}y &= ac^x \\y &= 8192 (0.5)^{12} \\y &= 2\end{aligned}$$

/ 3 pts

There will be 2 players left after the 12th round

4. You open an investment account at the **age of 25** with a deposit of **2750 \$**.

Your investment adviser tells you your money will **double every 6 years**.

How much money can you expect to have in your account when you retire at age 64?

$$x = \text{years } (64 - 25) = \frac{39}{6} = 6.5$$

$$y = \text{money}$$

$$a = 2750$$

$$c = 2$$

$$y = ac^x$$

$$y = 2750(2)^{6.5}$$

$$y = 248901.59$$

/ 3 pts

You can expect to have \$ 248 901.59 in the account

5. I have \$ 1503.51 in my account after 12 years investing at 3.5 % per year.

How much money did I start investing with?

$$y = ac^x$$

$$1503.51 = a(1.035)^{12}$$

$$\frac{1503.51}{1.51106865734} = \frac{a(1.51106865734)}{1.51106865734}$$

$$995 = a$$

$$x = \text{years } (12)$$

$$y = \text{money } 1503.51$$

$$a = ?$$

$$c = \frac{100 + 3.5}{100} = 1.035$$

/ 4 pts

I started investing with \$ 995

6. A painting was purchased in 2016 for 1.0 million dollars.

The value of the painting **increases by 6.5 % every year** from the date of purchase.

In what year will the value of the painting triple in value?

$$x = \text{years}$$

$$y = 3 \text{ million}$$

$$a = 1 \text{ million}$$

$$c = 1.065$$

$$y = ac^x$$

$$3 = 1(1.065)^x$$

X	Y
8	1.65
20	3.52
17	2.91
18	3.10

/ 4 pts

$$\begin{array}{r} 2016 \\ + 18 \\ \hline 2034 \end{array}$$

The painting will triple in value in the year 2034

7. Jess and Sam both started investing at the same time.

Jess started with 1200 \$ and her investment grew by 5% every year.

Sam started with 1600 \$ and her investment grew by 4% every year.

$$100 + 5 = \frac{105}{100} = 1.05$$
$$100 + 4 = \frac{104}{100} = 1.04$$

After a number of years, Jess' investment was worth 1772.95\$

How much profit did Sam make from her investment?

Hint: $\text{Profit} = \text{final money} - \text{initial money}$

Jess

$$y = ac^x$$

$$1772.95 = 1200(1.05)^x$$

x	y
5	1531.53
8	1772.95

Sam

$$y = ac^x$$

$$y = 1600(1.04)^8$$

$$y = 2189.71$$

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$$2189.71 - 1600 = 589.71$$

Answer: Sam made a profit of \$ 589.71 from her investment.